

Holiday Variable Generating Routines Within Our In-House Versions of the Census Method.

Holiday adjustment is an important part of seasonal adjustment. But it is often hard to measure. I would like to introduce the way we have been applying. Also, I would like to talk about the current plan for the routines to build in X-13ARIMA-SEATS.



## Hideki Furuya

Vice President and Chief Economist, SKANIOGLOS Investment Advisory Company Limited  $^{\dagger}$ 

Certified Member Analyst of the Securities Analysts Association of Japan Member of Pan Pacific Association of Input-Output Studies

<sup>†</sup>Registered Financial Instruments Business Operator in Tokyo, which provides macro-economics driven investment strategies on global securities/currencies portfolios.

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Hideki Furuya is Vice President and Chief Economist of SKANIOGLOS Investment Advisory Company Limited. SKANIOGLOS Investment Advisory is a Registered Financial Instruments Business Operator in Tokyo, which provides macro economics driven investment strategies on global securities currencies portfolios.



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Major holidays often affect to the country where the holidays are not publicly celebrated. This is an example to detect Chinese Year Factor from the industrial production index of the United States. This is the original series, or the series not seasonally adjusted yet.



Adjusted for the lengths of Februarys.



Leap year adjustment.



Seasonal factor and leap year factor are plotted as one dotted line. They are removed from the solid line. But holiday factors are not removed yet.



Easter factor.



Labor day factor.



Thanksgiving Christmas factor. These factors were estimated and removed.



Original Census Method can do this.



Let the scale be changed for these holiday factors to compare with Chinese New Year factors. Because from earlier this century, industrial productions of many advanced countries often show fluctuations on January and February.



Easter factor is the largest among these three holiday factors. Years like 2013, 16, 18, March productions were down by -0.65% and April productions were up by +0.65% as holiday effect. Therefore, month on month basis, holiday factor pushed up April monthly growth by 1.3%.



Chinese New Year effect is divided into two factors. One is Pre Chinese New Year factor, to trace surge of production prior to the holiday.



Two is Chinese New Year factor, to trace low production period amid and after the holiday.



Chinese New Year factors were accepted by the AIC test of the Census Method. Magnitudes of them are not so different from the Easter, as charted in the lower part of this figure. Let us look at the lower part of this chart, holiday factors for a while.



Pre Chinese New Year factor and Chinese New Year factor cross out each other. Let the product of both factors to name Total Chinese New Year factor.



Easter factor occurs on March and April in this model. For other months, value of Easter factor is 100% which means neutral. Chinese New Year factor occurs from December to February, and other months are 100% in this model.



Upper part is level of holiday factors. Lower part is month on month change of holiday factors. For the years 2017, 20, 21, and year 2023, Total Chinese New Year factor is estimated to be larger than Easter factor. For the purpose of, say, international comparison of equally adjusted series, Chinese New Year would be a candidate.



Then, how the Chinese New Year factors were estimated while there are no such official holidays in the USA?

1. Detection of holiday effects (4)	
Modelspan = (2000.01, 2022.03) Aictest = (user). # Note that additional holiday regressors are generated as user holiday variab Easter[8] $\times$ Labor[8] $\times$ Thanksgiving[1] factors $\Diamond$	les.
Pre Chinese New Year window O higher production; start: Monday on or right before [0101(-22)],	
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Pre holiday window, written in the rounded rectangle, starts at Monday, on or right before, the 22 days earlier than Chinese New Year.

1. Detection of holiday effects (4)	
Modelspan = (2000.01, 2022.03) Aictest = (user). # Note that additional holiday regressors are generated as user holiday variab Easter[8] $\times$ Labor[8] $\times$ Thanksgiving[1] factors $\Diamond$	les.
Pre Chinese New Year window O higher production; start: Monday on or right before [0101(-22)], end: 8 days earlier than the New Year Day [0101(-8)].	
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Pre holiday window ends at eight days earlier than the Chinese New Year.

1. Detection of holiday effects (4)	
Modelspan = (2000.01, 2022.03) Aictest = (user). # Note that additional holiday regressors are generated as Easter[8] × Labor[8] × Thanksgiving[1] factors ◇	user holiday variables.
Pre Chinese New Year window O higher production; start: Monday on or right before [0101(-22)], end: 8 days earlier than the New Year Day [0101(-8)].	
Chinese New Year window △ lower production; start: 7 days earlier than the New Year Day [0101(-7)],	
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Holiday window, in the rectangle, starts at seven days earlier than the Chinese New Year.

1. Detection of holiday effects (4)	
Modelspan = (2000.01, 2022.03) Aictest = (user). # Note that additional holiday regressors are generated as Easter[8] × Labor[8] × Thanksgiving[1] factors ◇	s user holiday variables.
Pre Chinese New Year window () higher production; start: Monday on or right before [0101(-22)], end: 8 days earlier than the New Year Day [0101(-8)].	
Chinese New Year window △ lower production; start: 7 days earlier than the New Year Day [0101(-7)], end: the 1 <sup>st</sup> Sunday from the second day of New Year [0102].	
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Holiday window ends at the first Sunday on or right after new year the second.

1. Detection of holiday effects (4)	
Modelspan = (2000.01, 2022.03) Aictest = (user). # Note that additional holiday regressors are generated as u Easter[8] × Labor[8] × Thanksgiving[1] factors <>	ıser holiday variables.
Pre Chinese New Year window O higher production; start: Monday on or right before [0101(-22)], end: 8 days earlier than the New Year Day [0101(-8)].	
Chinese New Year window △ lower production; start: 7 days earlier than the New Year Day [0101(-7)], end: the 1 <sup>st</sup> Sunday from the second day of New Year [0102].	Lower AICC than else.
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These windows were selected from various windows because they had lower AICCs than other windows. How these windows were chosen?



Use of model selection criteria is explained in the section 5.5 of the reference manual.



That is the former half of the story, holiday effects which dates are not public holiday. And the story continues to the latter half.



PDF version of this slide, with references, will be uploaded to our corporate website. Also, reports on development of enhanced X-13ARIMA-SEATS will be uploaded.

RegARIM. section 5.5 https://ww	A model. See further details for chapters 4 and 5 of the Reference Manual, especially, chapter 5 "Use of model selection criteria". w2.census.gov/software/x-13arima-seats/x13as/unix-linux/documentation/docx13ashtml.pdf	ò,
1. Fix ot	ner things being equal.	
1.1.	to AICC comparable	
1.1.1.	Fix outlier regressors. Do not use outlier { }.	
1.1.2.	Fix differencing operators like arima{ model=(011)(011)12 }.	
1.2.	Fix other regressors (td, Easter, etc.) which usually applied.	

The story continues. Procedure of detection can be divided into three steps. One. Outliers, differencing operators, and other regressors which usually applied should be fixed.

## 2. Procedure

RegARIMA model. See further details for chapters 4 and 5 of the Reference Manual, especially, chapter 5, section 5.5 "Use of model selection criteria". https://www2.census.gov/software/x-13arima-seats/x13as/unix-linux/documentation/docx13ashtml.pdf

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2. Compare AICCs of holiday regressors and choose one.

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#### Two. Compare various holiday regressors and choose one.

## 2. Procedure

RegARIMA model. See further details for chapters 4 and 5 of the Reference Manual, especially, chapter 5, section 5.5 "Use of model selection criteria". https://www2.census.gov/software/x-13arima-seats/x13as/unix-linux/documentation/docx13ashtml.pdf

- 1. Fix other things being equal.
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- 2. Compare AICCs of holiday regressors and choose one.
- 3. Apply chosen holiday regressors and estimate with automodel or other automatic selections if needed.

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Three. Apply chosen holiday regressors and estimate with automatic selections if needed.

3. Holiday windows	
Holiday windows are the dates which are assumed to be affected by the holiday.	
Ex. 1, begins at the New Year's Eve, ends at the 3 <sup>rd</sup> of the New Year. Ex. 2, begins at the 3 <sup>rd</sup> Monday prior to the day before New Year's Eve, ends at the day before Ne	w Year's Eve.
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Holiday windows are the dates which are assumed to be affected by the holiday. For example one. A window begins at the New Year's Eve, and ends at the third of the New Year. Example two. A window begins at the third Monday prior to the day before New Year's Eve, and ends at the day before New Year's Eve.

<ul><li>Holiday windows are the dates</li><li>Holiday windows are not neces</li><li>Public holiday dates are ofte</li><li>Chinese New Year effects ca</li></ul>	which are assumed to be affected by the holiday. sarily equal to public holiday. en rejected by the AIC tests. In be observed for the countries without public holidays.	
For such cases;		

Holiday windows are not necessarily equal to public holiday. Public holiday dates are often rejected by the AIC tests. Chinese New Year effects can be observed for the countries without public holidays.

# 3. Holiday windows

Holiday windows are the dates which are assumed to be affected by the holiday.

Detection of unknown holiday windows;

three regressor model:  $y_t = \beta' X_t + \sum_{i=1}^3 \alpha_i H_i(\tau, t) + z_t$ ,

where,  $y_t = \ln Y_t$ , logarithm of the original series,

 $\beta' X_t,$  other regressors, say, trading day regressors, or other holiday regressors,

 $\alpha_i H_i(\tau, t)$ , holiday regressors of the period t, which month in Gregorian calendar is  $\tau$ ,

pre-holiday  $H_1(\tau, t) = N_1(\tau, t)/N_1(\tau)$ , phase of higher production prior to the holiday,

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For the detection of unknown holiday windows, three-regressor model may be applicable. The first of three regressors is for pre-holiday, the phase of higher production prior to the holiday.

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## 3. Holiday windows

Holiday windows are the dates which are assumed to be affected by the holiday.

Detection of unknown holiday windows;

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pre-holiday  $H_1(\tau, t) = N_1(\tau, t)/N_1(\tau)$ , phase of higher production prior to the holiday,

peri-holiday  $H_2(\tau, t) = N_2(\tau, t)/N_2(\tau)$ , phase of low production during the holiday,

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The second of three regressors is for peri-holiday, the phase of low production during the holiday.

## 3. Holiday windows

Holiday windows are the dates which are assumed to be affected by the holiday.

Detection of unknown holiday windows;

three regressor model:  $y_t = \beta' X_t + \sum_{i=1}^3 \alpha_i H_i(\tau, t) + z_t$ ,

where,  $y_t = \ln Y_t$ , logarithm of the original series,

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 $\alpha_i H_i(\tau,t),$  holiday regressors of the period t, which month in Gregorian calendar is  $\tau,$ 

pre-holiday  $H_1(\tau, t) = N_1(\tau, t)/N_1(\tau)$ , phase of higher production prior to the holiday,

peri-holiday  $H_2(\tau, t) = N_2(\tau, t)/N_2(\tau)$ , phase of low production during the holiday,

post-holiday  $H_3(\tau, t) = N_3(\tau, t)/N_3(\tau)$ , phase of recovery of production after the holiday,

 $N_i(\tau, t)$ , number of dates within above phase in the period t, which month is  $\tau$ ,

 $N_i(\tau)$ , long-term average of  $N_i(\tau, t)$  which month is  $\tau$ ,

and,  $z_t$ , residual to follow ARIMA process.

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The third of three regressors is for post-holiday, the phase of recovery of production after the holiday.



Also, two regressor model can be applicable. The first of two regressors is for pre-holiday, the phase of higher production prior to the holiday.



The second of two regressors is for holiday, the phase of low production and recovery after the holiday.



Of course, one regressor model may be applicable.



Then, holiday window would be changed to holiday regressor by the program.



Let me explain about the procedure which has been applied. The first to fix is, border of holiday windows with a 7-day pre-holiday window and a 7-day holiday window.



Compare AICCs of various borders and, find the lowest. Of course the windows can be overlapped. But I prefer to separate the holiday periods.



Next, find start of pre-holiday window and end of holiday window.



Border of windows. If there exists public holiday, test three window models. Let the peri-holiday to be the public holiday dates.



And two window models. Let the beginning of holiday window as beginning of public holiday, or the weekend right before.



After fixing the beginning of pre-holiday window and the end of holiday window, compare the AICCs of best models and choose one.



If there are no public holidays and the series is affected via merchandise trade, border of holiday windows is unknown. Experimentally fix preholiday window and holiday window to 7 days. Move the border from several months earlier to several months later. Then, choose the lowest AICC as the border.



Hence, the border of holiday window is fixed.



Then, fix the start of pre-holiday window and end of holiday window, you can get regressors. This chart and coming charts trace the procedure to find holiday windows of the lowest AICC for industrial production of Taiwan.



This case, end of pre-holiday window was fixed as the day before New Year's Eve. Start of holiday window was also fixed as New Year's Eve.



Comparing various start of pre-holiday window, lower AICC's were seen among pre-holiday window, which start from, 30 days to 15 days preceding to the New Year's Eve.



End of holiday window. Lower AICC's were found among, 8 days to 16 days after the third day of the New Year.



End of holiday window continues. End of windows defined by day-ofweek had lower AICC's. Among them, end at the second Thursday after New Year the third was selected.



Start of pre-holiday windows were as well. From the fourth Saturday preceding to the New Year's Eve had the lowest AICC.

section 5.5 "Use of model sele https://www2.census.gov/softwa	ction criteria". are/x-13arima-seats/x13as/unix-linux/d	Reference Manual, especially, chapter 5, locumentation/docx13ashtml.pdf	
1. Fix other things being e	equal.		
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1.1.2. Fix differencing o	perators like arima{ model=(0)	11)(011)12 }.	
1.2. Fix other regresso	ors (td, Easter, etc.) which usuall	y applied.	
2. Compare AICCs of hol	iday regressors and choose one.	Stored in the file METAFILE.SLG.	]
3. Apply chosen holiday	regressors and estimate with au	tomodel or other automatic selections	
if needed.			
if needed.			

Let's back to the procedure section. Assume all the holiday regressors are tested. Also assume key statistics including AICC's, regressed parameters, and chosen models are stored into one file named meta file dot SLG. Choose one model from the low AICC group within this file.

## 2. Procedure

RegARIMA model. See further details for chapters 4 and 5 of the Reference Manual, especially, chapter 5, section 5.5 "Use of model selection criteria". https://www2.census.gov/software/x-13arima-seats/x13as/unix-linux/documentation/docx13ashtml.pdf

- 1. Fix other things being equal.
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Then, apply chosen holiday regressors and estimate with automatic selections if needed.

RegARIMA mo section 5.5 "Use https://www2.ce	del. See further details for chapters 4 and 5 of the Reference Manual, esp e of model selection criteria". ensus.gov/software/x-13arima-seats/x13as/unix-linux/documentation/docx13ash	ecially, chapter 5, .tml.pdf
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3. Apply cho	sen holiday regressors and estimate with automodel or other au	tomatic selections
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if needed.		
if needed.		
if needed.		

Note that above process needs to compare several thousands of regressors for each holiday.

RegA section https:	ARIMA model. See further details for chapters 4 and 5 of the Reference Manual, especially, chapter 5, on 5.5 "Use of model selection criteria". //www2.census.gov/software/x-13arima-seats/x13as/unix-linux/documentation/docx13ashtml.pdf	
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2. C	Compare AICCs of holiday regressors and choose one. Usually several 1000s of regressor	rs.
3. A if	Apply chosen holiday regressors and estimate with automodel or other automatic selections f needed.	
Dete	ction of "the World's major moving holiday factors": several hours for each series.	

Detection of the World's major moving holiday factors would need several hour calculation for each series.

кеş sec httŗ	gARIMA model. See further details for chapters 4 and 5 of the Reference Manual, especially, chapter 5, :tion 5.5 "Use of model selection criteria". ps://www2.census.gov/software/x-13arima-seats/x13as/unix-linux/documentation/docx13ashtml.pdf
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De	etection of "the World's major moving holiday factors": several hours for each series
<u></u>	Efficient processes are welcome

Therefore, efficient processes are welcome.

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De	etection of "the World's major moving holiday factors": several hours for each series.
$\checkmark$	Efficient processes are welcome.
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I will automate above process for easier detections.



Data of the following calendars and holidays have been prepared to build in X-13ARIMA-SEATS. Very roughly from east to west; Matariki holiday of Maori New Year: Korean, Chinese, and Vietnamese variants of Chinese type lunisolar calendar: Thai variant of Buddhist calendar: Deepavali and other holidays of Hindu calendar: Hijiri lunar calendar: Hebrew lunisolar calendar: Liturgical calendars of Eastern and Western Christianity.



There remains lots of stories about enhancement of the Census Method. Mr. Takashi Suga began to develop When\_exe in the mid 1990s. When\_ exe is a library of all the calendars which have ever appeared, planned, or imagined in the history. This is the source of my idea for a module to remove the World's major moving holiday factors.



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Links to articles, formulae,

6. References and links (2)				
Hindu festivals: <u>https://www.drikpanchang</u> .	<u>com/</u> . Among the panchang sites, span of this site is extremely long.			
$\{1001 \text{ years from } 1600 \text{ to } 2600 + (10 \text{ year } 1600 \text{ sole}) = 28,872. At least, 28,872 times.$	backcast span + 10 year forecast span) + (maximum 1 year lead + maximum 1	year lag)} × 6 cities × 4 holidays		
The Gregorian Calendar was introduced to se stated as three appropriate that	et proper dates of Easter (ad rectam Paschalis festi). In the today's title "Inter Graviss	imas", Pope Gregory XIII		
first, correct placement of ti next, correct placement of t equinox itself or is the next to	he vernal equinox; <b>The first condition is, March equinox to fall around M</b> the fourteenth day of the moon in the first month, which [fourteenth day] either follow after;	<b>arch 21<sup>st</sup>.</b> occurs on the day of the		
<ul> <li>and lastly, the first Sunday Photocopy of Clavius, Christoph, Romani Calenda Calendarium aliter instaurandum esse contender was taken from</li> </ul>	which follows that same fourteenth day of the moon. rii A Gregorio XIII. P. M. restitvti explicatio S. D. N. Clementis VIII. P. M. Ivssvedita : acce runt, 1603	sit confutatio eorum, qui		
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Euro area and EU working days to build Ca	alendar Adjustment Regressor			
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And important sites will be stored in the pdf version of this slide.



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